Dynamic RCS Estimation according to Drone Movement Using the MoM and Far-Field Approximation

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Abstract

Micro-Doppler signatures from the rotating propellers of a drone can be utilized to distinguish the drone from clutter or airborne organisms with similar radar cross section (RCS) levels, such as birds and bats. To obtain the micro-Doppler signatures of a drone, calculation or measurement of the electric field scattered from the rotating propellers is essential. In this paper, using the relative angle concept and far-field approximation, we propose a way to rapidly estimate the dynamic RCS of a drone with several propellers according to its movement. In addition, based on the fact that the shape of the propeller does not change even if it rotates, we construct an impedance matrix only once and apply the matrix to the method of moments instead of the iterative process of calculating the impedance matrix and inverse matrix for each rotation angle of the propeller. Finally, by using the Fourier transform of the results from the proposed method, the rotation frequencies of the propellers according to the movement of the drone can be obtained.

Key Words: Drone, Method of Moments (MoM), Micro-Doppler, Radar Cross Section (RCS), Rotation Frequency.

I. INTRODUCTION

Recently, the use of drones has been increasing due to their drop in price and miniaturization. At the same time, drones can be abused, leading to issues like privacy violations. Moreover, there is the risk of collision, and they could also be used to transport illegal materials. However, conventional security systems are generally vulnerable to undetected small targets in the air; hence, interest in drone detection technology has increased.

Radar is an appropriate technology for detecting or tracking a target using its radar cross section (RCS). Therefore, early studies on drone detection mainly focused on estimating or measuring the RCS level of drones as well as airborne organisms that have an RCS level similar to that of drones [1]. Despite the existence of many such studies, the RCS level-based method still has difficulties in distinguishing drones from airborne organisms [2]. To solve this problem, methods based on the signature extracted from the RCS of a target rather than the simple RCS level have been studied [3–13]. Inverse synthetic aperture radar (ISAR) images of small drones were investigated in [4]. Two- and three-dimensional ISAR images of drones are also used to classify drones. On the other hand, the micro-Doppler signatures induced by the flapping of various birds' wings have been also investigated [5, 6]. Additionally, in [7–10], the authors showed the difference between the micro-Doppler signatures of flapping bird wings and rotating drone propellers.

To obtain these micro-Doppler signatures for the detection and tracking of a drone, the measurement or estimation of electric
fields scattered from the drone’s propellers with respect to time is essential. Early studies mostly used the measured dynamic RCS—the squared magnitude of the scattered field with respect to time—because the estimation of the dynamic RCS from rotating propellers requires a large amount of computation time and resources. The measured dynamic RCS is realistic, but it is difficult to measure RCSs according to various drone situations. For this reason, the dynamic RCSs of drones have been generally only measured from hovering drones remaining in the same position. However, in [10], the authors showed that the dynamic RCSs of drones at aspect angles of 0° and 90° are considerably different—that is, the dynamic RCS of a drone is greatly affected by the observation angle. However, it is not easy to measure the dynamic RCS of a drone in the air from various angles.

In conventional commercial electromagnetic (EM) tools, the method of moments (MoM) solver generally performs a series of procedures, specifically mesh generation, construction of the impedance and admittance matrices, and calculation of the scattered field and RCS of a target. For the dynamic RCS of the rotating propellers of a drone, it is assumed that the quasi-static mode is established on a frame-by-frame basis with sampling intervals instead of a time-continuous model [11]. Therefore, MoM solvers repeatedly perform identical procedures for each frame. A substantial amount of time is needed to estimate the dynamic RCS of rotating propellers. Even though the propellers rotate, the shape of the propellers does not change; only the incident and scattered angles change. Therefore, using the relative angle between a rotating propeller and the incident field, mesh generation can be done just once along with the construction of the impedance and admittance matrices. Moreover, if the characteristics of the fields scattered from two types of drone propellers—clockwise (CW) and counter-clockwise (CCW) propellers—and far-field approximation are used, the fields scattered from all of the propellers can be synthesized with the scattered field of a single rotating propeller. This can result in a dramatic reduction in the calculation time.

II. PROPOSED METHOD TO ESTIMATE DYNAMIC RCS OF ROTATING PROPELLERS

1. Dynamic RCS of a Single Propeller

To calculate the electric field scattered from a single rotating propeller, MoM solvers in commercial EM tools perform a series of procedures sequentially, as shown in Fig. 1(a). The most time-consuming components of these MoM procedures are filling the impedance matrix and then converting it into an admittance matrix. It is well known that the impedance matrix in the MoM is constructed from the interaction among the mesh elements of a scatterer. Therefore, if the mesh is maintained while the scatterer is rotated, the impedance matrix does not change. That is, the mesh and the impedance matrix generated only once can be used continuously for a rotating propeller. As shown in Fig. 1(b), we reversely rotate the incident angle of the incident field in the rotation direction of the propeller instead of rotating the propeller, and its effect reflects on the excitation vector. Consequently, the current on the elements and the scattered field can obtained.

The electric field scattered from a propeller rotating clockwise, as shown in Fig. 2(a), can be expressed as

\[ E^s(t; \theta_{inc}, \phi_{inc}) = S_{CW}(t) \cdot E^i(\theta_{inc}, \phi_{inc}), \]

where \( S_{CW}(t) \) and \( E^i \) are the scattering matrix of the CW rotating propeller and the incident electric field, respectively. Instead of rotating the propeller, if the incident azimuth angle, \( \phi_{inc} \), is rotated in the direction opposite to the rotation direction of the propeller, thus keeping the incident elevation angle, \( \theta_{inc} \), fixed,

![Fig. 1. Flow chart to estimate RCS of a drone with (a) conventional and (b) proposed methods.](image)

![Fig. 2. Two types of drone propellers: (a) CW and (b) CCW.](image)
the same scattered field as Eq. (1) can be obtained by
\[
E^z(t; \theta_e, \phi_e) = S^{cw} \cdot E^{ccw}(\theta_{inc}(t), \phi_{inc}(t)).
\] (2)

On the other hand, drones commonly consist of two types of propellers, namely, mirror-image symmetric CW and CCW propellers, as shown in Fig. 2. CW and CCW propellers rotate only clockwise and counter-clockwise, respectively. Because of their mirror-image symmetric characteristics, the co-polarized components of the electric fields scattered from CW and CCW propellers are the same, and the cross-polarized components have a phase difference of 180°. Therefore, the scattering matrices of the two types of propellers have the following relationship:
\[
\begin{bmatrix}
S^{cw}_{\theta \theta} & S^{cw}_{\theta \phi} \\
S^{cw}_{\phi \theta} & S^{cw}_{\phi \phi}
\end{bmatrix} = \begin{bmatrix}
S^{cw}_{\theta \theta} & -S^{ccw}_{\theta \phi} \\
-S^{ccw}_{\phi \theta} & S^{ccw}_{\phi \phi}
\end{bmatrix}.
\] (3)

From Eq. (3), the electric field scattered from one type of propeller can be easily obtained from the electric field scattered from the other type without additional calculations.

2. Dynamic RCS of Multiple Propellers

The geometry of a radar and a drone with 4 propellers is presented in Fig. 3(a). Let us assume that the origin, \(O\), of the reference coordinate is the center of the drone, and the \(n\)th propeller and the radar are located at \(T_n\) and \(P_1\), respectively. If the radar, which faces the head of the drone, is far from the drone, then the backscattered field at the far-field can be approximated as
\[
E^z_i(t) \equiv \sum_{n=1}^{4} E^z_{i_n}(t; \theta_{P_1}, \phi_{P_1}) \cdot \exp(-j2k \cdot \bar{r}_n),
\] (4)
where \(E^z_{i_n}\) is the backscattered field of the \(n\)th single propeller when the center of the propeller is located at the origin \(O\), and \(\theta_{P_1}\) and \(\phi_{P_1}\) are the elevation and azimuth angles of the incident field from \(P_1\), respectively, where \(\phi_{P_1} = 0\) because of the radar located in the heading direction. Here, \(\bar{r}_n\) is the position vector of the \(n\)th propeller's center, and \(k\) is the wave number vector for the operating frequency, \(f_i\) and is defined as \(|\bar{P}_1O|\).

Finally, the RCS of the multiple propellers can be estimated by
\[
RCS = \lim_{R \to \infty} 4\pi R^2 \frac{|E^z|^2}{|E|^2}.
\] (5)

3. Dynamic RCS of Multiple Propellers in the Azimuth Plane

Because a radar can be oriented in any direction, the RCS estimation of multiple propellers for the arbitrary azimuth angle is needed. Let us assume that the observation point is changed from \(P_1\) to \(P_2\) by changing only the azimuth angle from \(\phi_{P_1}\) to \(\phi_{P_2}\) while maintaining the elevation angle, \(\theta_{P_1}\). The incident and scattered angles is included in \(E^z_{i_n}(t; \theta_{P_1}, \phi_{P_1})\) as well as \(\bar{k}\) of Eq. (4). If only the wave vector \(\bar{k}\) is updated with the moved observation point, the initial direction of the propellers is directed toward \(P_2\), as shown in Fig. 4(a). This is because the changed angle information is not updated to the scattered field of each propeller, so the initial direction of the propellers is toward the incident wave direction. However, the desired direction of the propellers should be the heading direction as shown in Figs. 3(b) and 4(b). In order to update the changed angles into the scattered field, it is not necessary to recalculate the backscattered field, but only to change the rotation starting angle of \(E^z_{i_n}\) depending on the propeller type, because the backscattered field, \(E^z_{i_n}(\theta_{P_n}, \phi_{P_n})\), was calculated when the single propeller was rotated once. According to the changed azimuth angle, the backscattered fields can be obtained by
\[
E^z_{i_n}(\theta_{P_n}, \phi_{P_n}) = \begin{cases} E^z_{i_n}(\theta_{P_n}, \phi_{P_n} + \phi_{obs}), & \text{for CW propeller} \\ E^z_{i_n}(\theta_{P_n}, \phi_{P_n} - \phi_{obs}), & \text{for CCW propeller} \end{cases},
\] (6)
where \(\phi_{obs}\) is the angle between \(\overline{OP_2}\) and the drone’s heading direction. The backscattered field of the multiple propellers for the arbitrary azimuth angle can be synthesized using Eq. (4). As a result, the direction of the radar can be not only at the front but also at the aspect of the drone.
III. RESULTS AND DISCUSSION

The proposed method is implemented based on the MoM with a Rao-Wilton-Glisson (RWG) basis function using the electric field integral equation (EFIE). Since only the impedance matrix for a single propeller of the drone is used in our simulation, the calculation of the admittance matrix, which is an inverse matrix of the impedance matrix, is not time-consuming. Therefore, the admittance matrix was calculated simply using Gauss elimination rather than iterative methods, such as the conjugate gradient algorithm, the biconjugate gradient algorithm, and the generalized minimal residual method.

To verify the proposed method, the monostatic dynamic RCSs of rotating propellers were calculated and compared with the results obtained from a commercial EM tool. First, the radar operating frequency and pulse repetition frequency were set to 9.65 GHz and 20 kHz, respectively, in reference to existing radar specifications [12–14]. Next, we choose DJI’s Mavic2 [15], which is one of the most popular drones, as the simulation drone model. Since the micro-Doppler is mainly generated by rotating the propellers, we used a computer-aided design (CAD) model of propellers alone without the main body in the simulation. Each propeller was 20.32 cm long (which results in about 6.5k at 9.65 GHz) and was made of carbon fiber. Because the dynamic RCSs of propellers with carbon fiber and a perfect electric conductor (PEC) are very similar in terms of RCS level and patterns [16, 17], the material of the propellers was simply assumed to be the PEC.

1. Single Propeller

The electric fields scattered from a single propeller rotating once a second were calculated at 0.1° intervals for one second. The backscattered fields with respect to the transmitting and receiving polarizations are shown in Figs. 5 and 6. In the case of co-polarization (θ−θ and φ−φ polarizations), the backscattered fields of the CW and CCW propellers are identical, while the fields of with cross-polarization (θ−φ and φ−θ polarizations) are inverse of each other because of their mirror-symmetric shape and rotation in opposite directions. Their polarimetric characteristics can be used to derive the backscattered field from the other propellers by simply calculating the backscattered field of only one propeller. Therefore, with more propellers, the time for calculating the backscattered field can be reduced.

Fig. 7 shows the dynamic RCSs of the two types of propellers. The proposed method was implemented using MATLAB, and the MoM solver of Altair’s FEKO was used as the conventional method. We performed all the simulations using a PC with Intel Core i7-8700 at 3.20 GHz and 64 GB RAM. There was little deviation in the results. As expected, since the proposed
method makes the admittance matrix only one time during the observation time (or dwell time), the proposed method considerably reduces the calculation time of a single propeller in comparison with the conventional method, as summarized in Table 1.

2. Multiple Propellers of Ascending Drone

We also simulated a case in which the radar was located in front of a drone with four propellers rotating at 156.6 Hz, as shown in Fig. 3(a), and the elevation and azimuth angles of the incident field were 45° and 0°, respectively. The dynamic RCSs and backscattered spectrum were calculated during one rotation period. Fig. 8(a) shows the dynamic RCS of the ascending drone. The proposed method was implemented with the procedure shown in Fig. 1(b), while the conventional method, FEKO’s MoM solver, was performed at every time step using the procedure shown in Fig. 1(a). As a result, it took a large amount of time to estimate the dynamic RCS of the multiple propellers. Therefore, the conventional method for estimating the dynamic RCS of multiple propellers was implemented using FEKO’s multilevel fast multipole method (MLFMM) solver. Fig. 9 shows the frequency response with the application of fast Fourier transform to the dynamic RCS. The frequency of the first peak is 313.2 Hz, which is twice as high as the rotation frequency because the two scattering points at both ends of the propeller rotate.

Fig. 8(b) shows the dynamic RCS when the radar is looking at the aspect of the drone at \( \phi_{\text{as}} = 70^\circ \). Compared to the front-looking case of Fig. 8(a), the dynamic RCS pattern is considerably changed. However, the back-scattered spectrum is similar. The first peak frequency is also 313.3 Hz, as shown in Fig. 9(b), which means the rotation frequency can be successfully obtained from the frequency-domain of the dynamic RCS.

3. Multiple Propellers of Advancing Drone

In considering a drone moving forward with the two front propellers rotating more slowly than the two back propellers, we set the rotation frequencies of the front and back propellers to 125.3 Hz and 156.6 Hz, respectively. The azimuth and elevation angles between the head of the drone and the radar were 0° and 45°, respectively. The dynamic RCS of the advancing drone is shown in Fig. 8(c), and the frequencies of the first and second peaks in Fig. 9(c) are 250.6 Hz and 313.3 Hz, respectively, which are twice as high as the rotation frequencies. However,
there is some discrepancy between the proposed and conventional methods in Fig. 9(c). This discrepancy seems to be due to the assumption that there is no coupling among the propellers for high-speed computation. For the quantitative analysis of the discrepancy, the normalized root-mean-square deviation (NRMSD) between the results of the proposed and conventional methods are summarized in Table 2. The NRMSDs between the results of the proposed method and conventional method are summarized in Table 2. Specifically, the NRMSDs are less than 2%, and the proposed method accurately estimates the dynamic RCSs of the four propellers. Above all, the proposed method considerably reduces the calculation time of the dynamic RCS 8 to 10 times compared with the conventional method, as seen in Table 3.

### IV. CONCLUSION

We introduced a MoM-based method to quickly estimate the dynamic RCSs of rotating objects. Conventional MoM solvers used in commercial EM tools repeatably construct the impedance matrix and its inverse matrix for a rotating object at every time interval, whereas the proposed method constructs the impedance matrix only once by rotating the incident angle instead of rotating the object. This core principle is applicable not only to drones but also to various objects with propellers [18, 19]. In addition, a multi-propeller dynamic RCS is synthesized via far-field approximation assuming that there is no coupling between the propellers and using the characteristics of two mirror-symmetric types of propellers used in drones. The proposed method can rapidly calculate a drone’s scattered fields from various angles, especially the aspect. From the estimated dynamic RCS, the rotation frequency of the propeller could be accurately obtained. Therefore, the proposed method can be effectively used to obtain the micro-Doppler of drones by estimating the dynamic RCS of various drone movements as well as various types of drones, such as drones with four or more propellers and drones with different sizes of propellers, to estimate the dynamic RCS of drone propellers with various materials in the future.

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### REFERENCES


### Table 2. NRMSDs of the difference between the results of the MoM and MLFMM from Fig. 8

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<thead>
<tr>
<th>Movement</th>
<th>NRMSD (%)</th>
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<tr>
<td>Ascent</td>
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<td>Ascent (aspect)</td>
<td>0.79</td>
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<td>Advance</td>
<td>1.03</td>
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### Table 3. Calculation time of dynamic RCSs according to the movement of the drone

<table>
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<tr>
<th>Movement</th>
<th>Time (hh:mm:ss)</th>
<th>Conventional</th>
<th>Proposed</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ascent</td>
<td>03:22:38</td>
<td>00:23:25</td>
<td></td>
</tr>
<tr>
<td>Ascent (aspect)</td>
<td>03:41:34</td>
<td>00:23:27</td>
<td></td>
</tr>
<tr>
<td>Advance</td>
<td>04:19:17</td>
<td>00:23:27</td>
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</table>
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